

# utomated short-run economic forecasts

(.)

bank of canada  
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# Introduction

- Motivation
- Global forecasts at the macroeconomic level
- Methodological framework
- Application for short-term growth
- Summary



## motivation

« ...policymakers are well advised to follow two principles familiar to navigators throughout the ages: first, determine your position frequently. second, use as many guides or landmarks as are available. »

Ernesto G. Fernanke, Michael J. Schatz

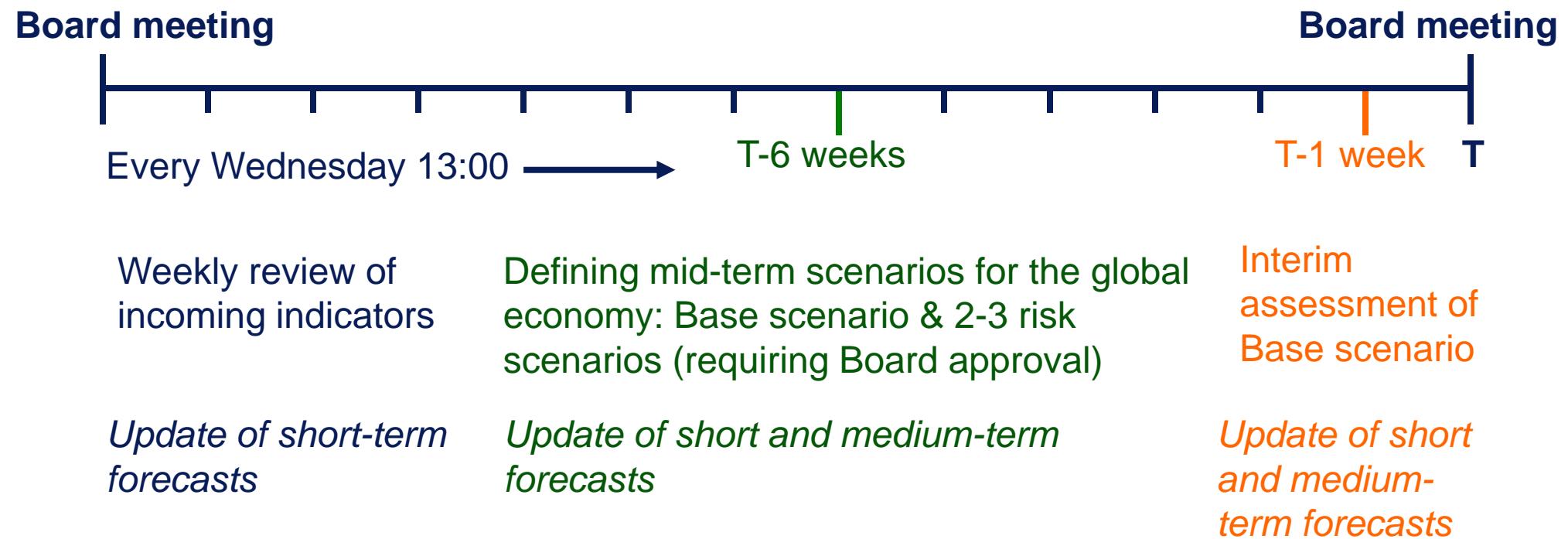
- ❖ Delays of the official value of ... and other national accounts data are published late
  - Global economic developments have to be assessed from numerous and more timely indicators
- ❖ Incorporate higher-frequency indicators into statistical, quantitative forecasting models
  - e.g. **Künstler** and **édillot** (), **ingenito** and **rehan** () ...
- ❖ Two main goals:
  - exploit the considerable amount of conjunctural information available before release of official national accounts data
  - build an automated process for an efficient day-to-day use

→ Project:

Automated procedure to select and run optimal, indicator models for short-term forecasting of the international economy

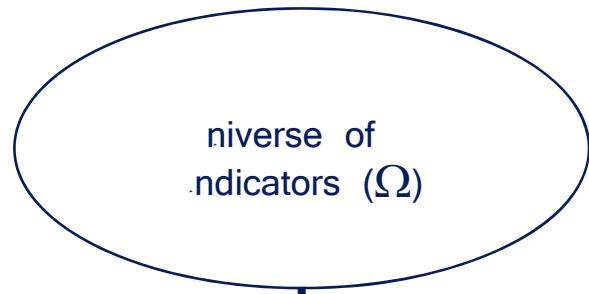
# • 's global forecasts cycle

Quarterly cycle: 13 weeks

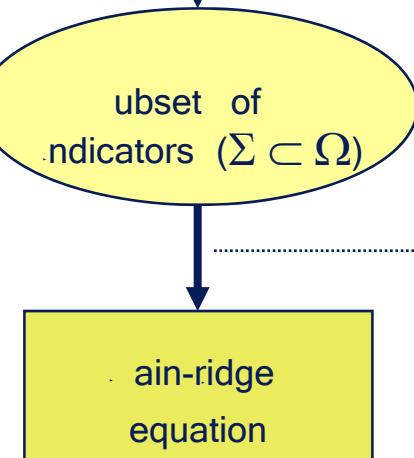


## . exicon

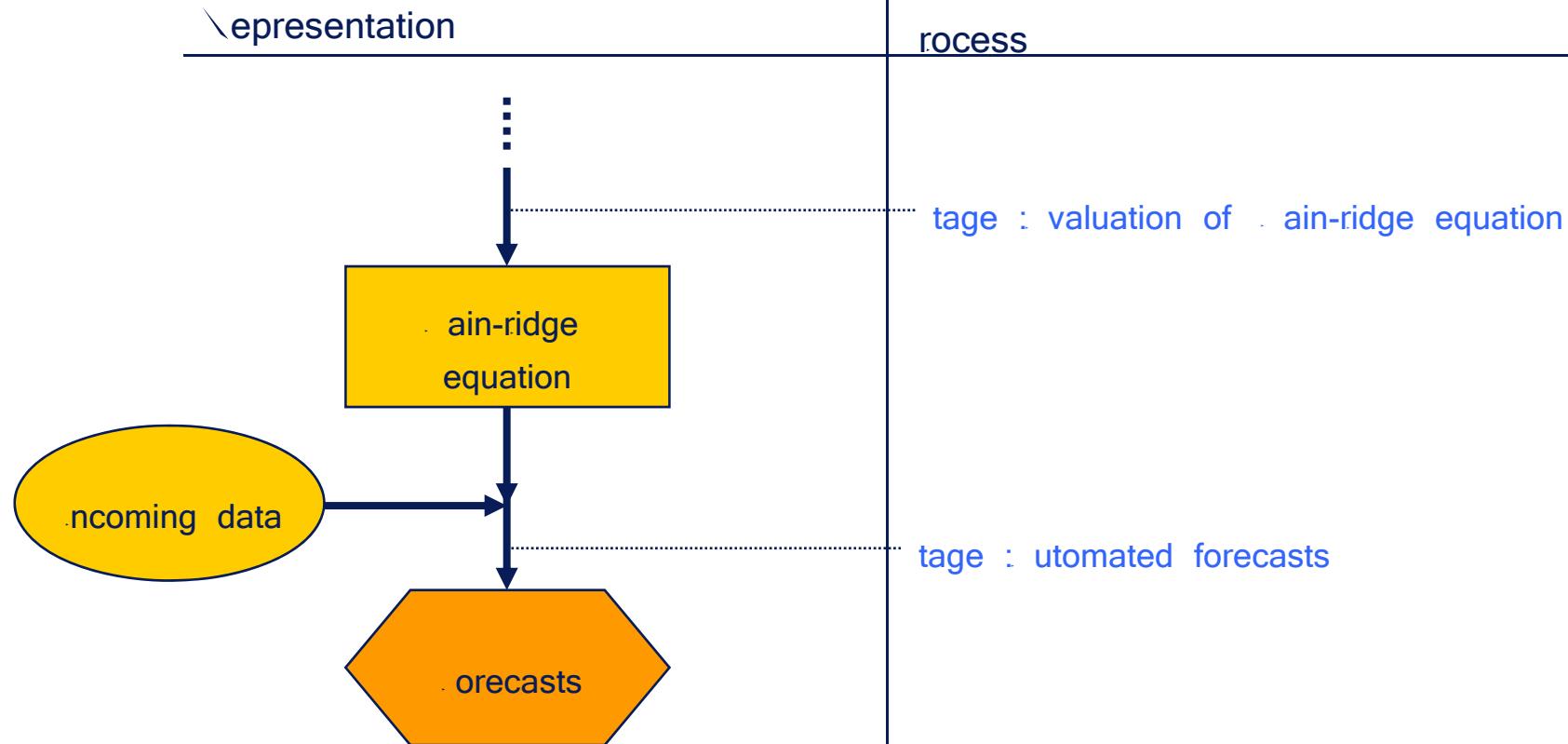
- ❖ . ain-ridge equation:
  - . forecast equation for the target variable (quarterly frequency)
- ❖ . ini-ridge equation:
  - . forecast equation for monthly indicators used as regressors in the . ain-ridge equation
- ❖ uxiliary variables:
  - . onthly indicators that appear in the . ini-ridge equations but not in the . ain-ridge equation
- ❖ ard indicators:
  - . uantitative data (e.g. industrial production, retail sales ...)
- ❖ oft indicators:
  - . ualitative data (e.g. usiness / consumer surveys...)

representationprocedure

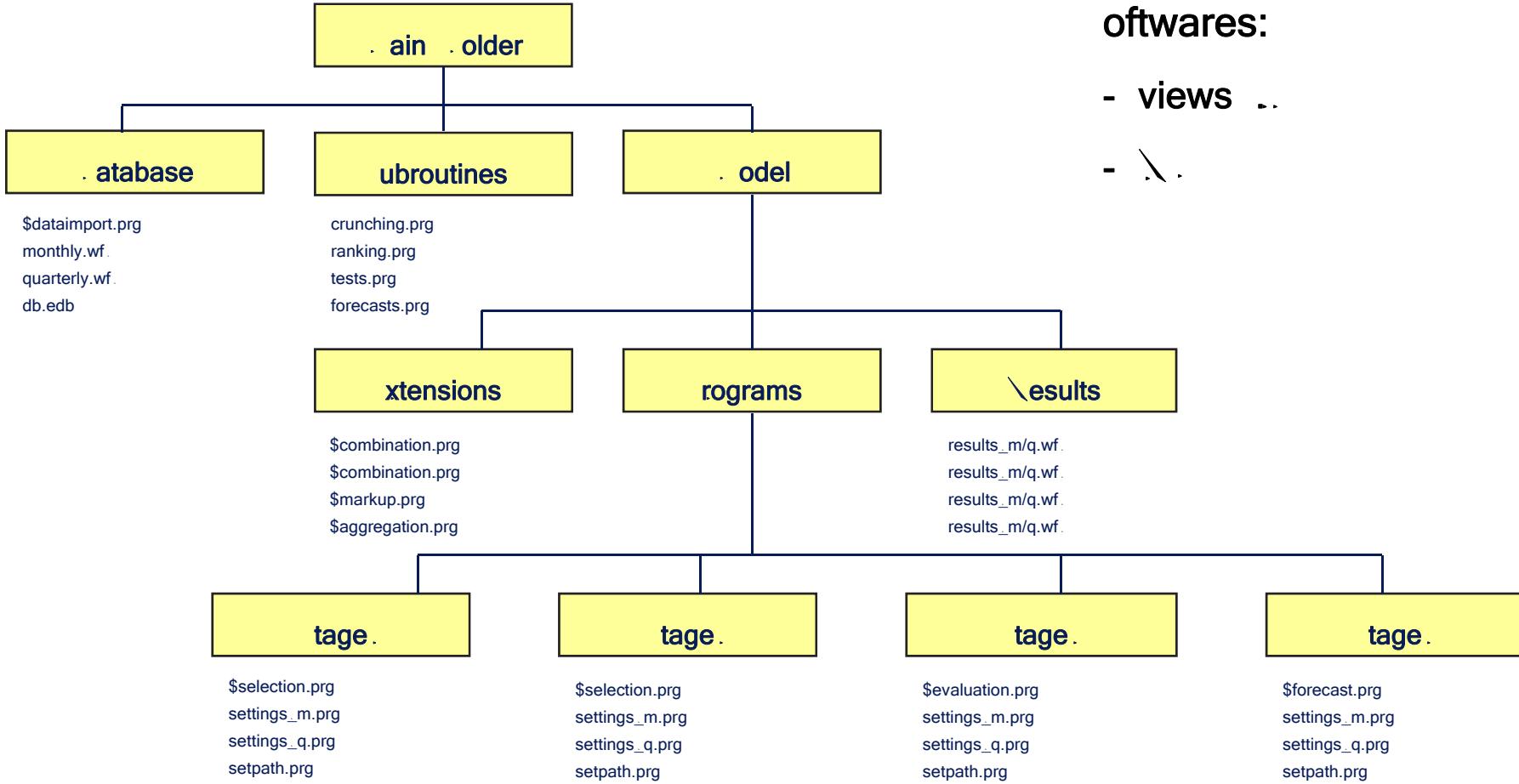
stage : indicator selection



stage : specification and estimation of the main-ridge equation



# structure



## stage : Indicator selection

- ❖ Ranks indicators according to their in-sample fit
- ❖ Test for potentially useful combination of forecasts (encompassing). Modified Diebold-Mariano  $t$ -test.

# stage : Indicator selection

- estimation of bivariate distributed lag regressions with lagged dependent variable
  - est lag specification for every stationary indicator  $x_{i,t}$
- ranking of the best models according to a specified criterion (., .. or adj. )
- encompassing bivariate tests (modified liebold-ariano  $t$ -test (arvey, eybourne and newbold, ) )
  - . - variables that contain additional information to the best single variable equation

## stage : application

- ❖ **target variable:** quarterly . . . growth (saar)
- ❖ **data set:** „hard“ indicators
- ❖ **max # of lags:** . (for exogenous); . (for target)
- ❖ **# of specifications:** .. (.x )
- ❖ **criterion:** adj. \
- ❖ **comp. time:** sec.



# Output: tage

EViews - [Table: SUMMARY1 Workfile: PROGRAMS1\_Q::results\]

	A	B	C	D	E	F
1	Variable	@RBAR2	Encomp Coeff	H0: lambda=0 p (corr)	H0: 1-lambda=0 p (corr)	Sample Range
2			--	--	--	
3	@PCA(IPMAN)	0.47290	--	--	--	1987 Q2 2007 Q2
4	IPDIFF3	0.43998	0.30034	0.37785	0.04838	1987 Q2 2007 Q2
5	@PCA(IP)	0.42988	-0.22824	0.63938	0.01450	1987 Q2 2007 Q2
6	@PCA(INITCLAIMS)	0.40179	0.29671	0.11396	0.00114	1987 Q2 2007 Q2
7	IPDIFF1	0.39894	0.20959	0.36416	0.00095	1987 Q2 2007 Q2
8	@PCA(IPDURCG)	0.39005	0.22417	0.26534	0.00056	1987 Q2 2007 Q2
9	@PCA(PRIVCONST)	0.38824	0.37001	0.00637	0.00015	1987 Q2 2007 Q2
10	@PCA(SHIPDUR)	0.38393	0.57369	0.08371	0.23670	1992 Q2 2007 Q2
11	D(CAPUTIL)	0.38343	-0.02983	0.92081	0.00471	1987 Q2 2007 Q2
12	@PCA(TOTHOURS)	0.37513	0.26585	0.13856	0.00036	1987 Q2 2007 Q2
13	@PCA(EMP)	0.37351	0.30537	0.05424	0.00000	1987 Q2 2007 Q2
14	IPDIFF6	0.36897	0.02868	0.91340	0.00081	1987 Q2 2007 Q2
15	@PCA(TOTCONST)	0.36578	0.34430	0.00864	0.00007	1987 Q2 2007 Q2
16	@PCA(SHIPDUREX...)	0.36297	0.50527	0.12517	0.17625	1992 Q2 2007 Q2
17	@PCA(PCE)	0.36091	0.35125	0.01550	0.00161	1987 Q2 2007 Q2
18	@PCA(EMPHHELP)	0.33925	0.26546	0.11802	0.00169	1990 Q2 2007 Q2
19	@PCA(HOUSSTART)	0.33083	0.30889	0.01712	0.00021	1987 Q2 2007 Q2
20	@PCA(PCENDUR)	0.31442	0.33300	0.02098	0.00005	1987 Q2 2007 Q2
21	@PCA(START1)	0.31401	0.28032	0.02977	0.00013	1987 Q2 2007 Q2
22	D(ISTOT)	0.31229	0.42251	0.10730	0.03368	1992 Q2 2007 Q2
23	@PCA(EMPSER)	0.30967	0.23602	0.11427	0.00000	1987 Q2 2007 Q2
24	@PCA(SHIPTOT)	0.30761	0.38519	0.18962	0.02249	1992 Q3 2007 Q2
25	@PCA(EX)	0.30721	0.43053	0.05108	0.00707	1994 Q4 2007 Q2
26	@PCA(PCEDUR)	0.30298	0.28858	0.03849	0.00025	1987 Q2 2007 Q2
27	UNEMP	0.29985	0.24184	0.07671	0.00015	1987 Q2 2007 Q2
28	@PCA(TOTHOURMAN)	0.29227	-0.09556	0.64512	0.00136	1987 Q2 2007 Q2
29	@PCA(RESCONST)	0.28967	0.36581	0.02779	0.00076	1993 Q2 2007 Q2
30	@PCA(TOTHOURC...)	0.28412	0.23041	0.07010	0.00000	1987 Q2 2007 Q2
31	@PCA(IPCG)	0.27881	-0.11840	0.56268	0.00000	1987 Q2 2007 Q2
32	@PCA(SHIPEXDEF)	0.27667	0.25796	0.36057	0.00842	1992 Q2 2007 Q2
33	@PCA(TOTHOURSE...)	0.27623	0.10699	0.50416	0.00001	1987 Q2 2007 Q2
34	@PCA(HELPWANT)	0.27401	0.19153	0.21275	0.00005	1987 Q2 2007 Q2
35	@PCA(SHIPCONDUR)	0.27272	0.33861	0.12831	0.00654	1992 Q2 2007 Q2
36	@PCA(IPBUSEQ)	0.27061	-0.20853	0.31031	0.00016	1987 Q2 2007 Q2
37	@PCA(NODUR)	0.26995	0.30254	0.17635	0.00591	1992 Q2 2007 Q2
38	@PCA(BUILDPERM)	0.26464	0.21509	0.08182	0.00008	1987 Q2 2007 Q2
39	D(BUSINVSAL)	0.26391	0.34622	0.11765	0.00917	1992 Q2 2007 Q2
40	@PCA(SHIPCAPEX...)	0.25531	0.32109	0.10767	0.01392	1992 Q2 2007 Q2
41	@PCA(IM)	0.25429	0.36163	0.07177	0.01572	1994 Q4 2007 Q2
42	@PCA(NOCONST)	0.25414	0.24012	0.33641	0.00806	1992 Q2 2007 Q2
43	@PCA(NODUREXDEF)	0.25319	0.19308	0.44734	0.01097	1992 Q2 2007 Q2
44	@PCA(NOTOT)	0.25314	0.24492	0.28795	0.00412	1992 Q2 2007 Q2
45	@PCA(EMPMAN)	0.25181	-0.09317	0.62156	0.00024	1987 Q2 2007 Q2
46	D(INVSALRA)	0.24834	0.36527	0.01658	0.00136	1992 Q3 2007 Q2
47	@PCA(SHIPCAPEX...)	0.24527	0.31498	0.13852	0.01343	1992 Q2 2007 Q2
48	@PCA(SHIPCAPEX...)	0.24512	0.29946	0.17308	0.01493	1992 Q2 2007 Q2
49	@PCA(SHIPCONST)	0.24443	0.21774	0.34446	0.00246	1992 Q2 2007 Q2
50	@PCA(DEFNSA)	0.24413	0.20800	0.11722	0.00000	1987 Q2 2007 Q2
51	@PCA(EXPCAP)	0.24396	0.29355	0.13181	0.00847	1994 Q2 2007 Q2
52	@PCA(IPINDEQ)	0.24057	-0.04651	0.80163	0.00009	1987 Q2 2007 Q2
53	@PCA(DEFENSE)	0.23902	0.21064	0.09487	0.00000	1987 Q2 2007 Q2
54						
	@PCA(IPMAN)					

tage :

dditional feature

- ❖ Possibility to use target also for a *monthly* target variable.

## tage :

### selection of the main-ridge equation

- ❖ find the optimal specification regarding lags and variables (e.g. selected from tage )
  
- ❖ the ranking is based on in-sample criteria (, , ...)

## stage .

### . ain-ridge equation

- ❖ . multivariate distributed lag regression with lagged dependent variable:

$$A(L)\Delta y_t = \beta_0 + \sum_{i=1}^S B_i(L)x_{i,t} + \varepsilon_t$$

→ est . ain-ridge equation

where regressors  $x_{i,t}$ : a subset of . indicators

## stage : pplication (contd)

- ❖ **Indicators:** .. manuf, .. and private constr.
- ❖ **sample:** q-q .
- ❖ **criterion:** ..
- ❖ **max. # of lags:** .. (exogenous); .. (target)
- ❖ **# of specifications:** .. ()
- ❖ **comput. time:** .. sec.

# output: tage

Table: SUMMARY3 Workfile: QUARTERL...

	A	B	C	D	E
1		@SCHWARZ	@SCHWARZ	@SCHWARZ	
2		1.	2.	3.	
3	Crit.	3.500750	3.508201	3.522736	
4	S.E.	1.240654	1.217204	1.224413	
5					
6	Models	@PCA(GDP)	@PCA(GDP)	@PCA(GDP)	
7		C	C	C	
8		@PCA(GDP(-1))	@PCA(GDP(-1))	@PCA(GDP(-1))	
9		@PCA(PCEM)	@PCA(PCEM)	@PCA(PCEM)	
10		@PCA(IPMAN)	@PCA(IPMAN)	@PCA(PCEM(-1))	
11		@PCA(PRIVCONST)	@PCA(PRIVCONST)	@PCA(IPMAN)	
12			@PCA(PRIVCONST(-2))	@PCA(PRIVCONST)	
13					
14					

## stage : additional features

- ❖ Possibility to find equations for variables in *monthly frequency*

## tage : main-ridge evaluation

- ❖ evaluate the forecast equation in pseudo out-of-sample exercises against . or . benchmarks
- ❖ input: . main-ridge (e.g. from tage ) and benchmark equations (e.g. univariate)
- ❖ output: . tests of forecasts properties

## stage :

### . tests

- *forecast accuracy*

est of mean squared errors equality. modified liebold-ariano *t*-test  
(arvey, eybourne and newbold, )

- *directional accuracy*

ests if the direction forecast is significantly different from a random draw. independence *hi-squared*-test. ( liebold and opez, )

- *forecast bias*

ests the null of unbiased forecasts. *t*- and *z*-test

- *normality of residuals*

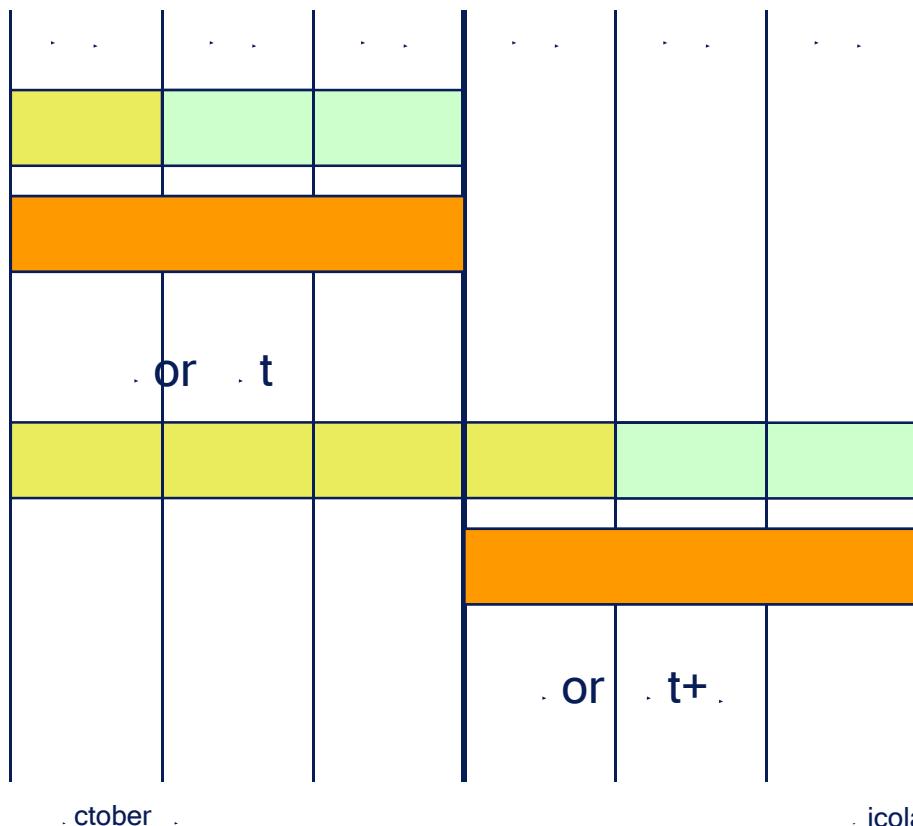
*arche-erra (hi-squared)* -test

## stage :

### main features

- ❖ Possibility to simulate different degree of information inside the quarter (. month, . months, full quarter)
- ❖ Values of exogenous variables are forecasted with a \ or the mean of the previous month(s)

# tage : rolling forecast (month of information)



- estimation (monthly)
- forecast (monthly)
- main-ridge forecast (quarterly)

tc...

# stage : application (contd)

- ❖ **ain-ridge ( . ):** pcha(gdp) c pcha(gdp(-)) pcha(pce) pcha(ipman)  
pcha(privconst)
- ❖ **enmark ( . \ . - . odel, rehan, ):** pcha(gdp) c pcha(gdp(-)) pcha(gdp(-))  
pcha(gdp(-)) pcha(pce) pcha(emp)
- ❖ **enmark :** est univariate for pcha(gdp) (up to . lags)
- ❖ **stimation period:** q . – q .
- ❖ **ut-of-sample forecast:** q-q . ( . obs.)
- ❖ **omputing time:** . sec.

# Output: tage

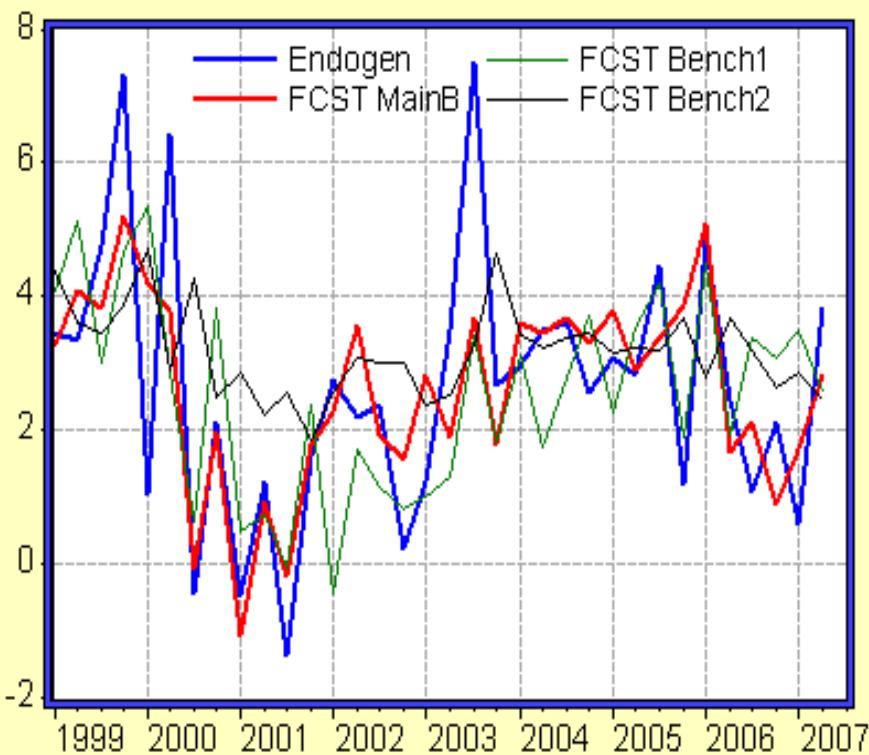


Table: SUMMARY\_TESTS Workfile: PROGR...

	A	B	C	D
	Best Model	Benchmark 1	Benchmark 2	
1				
2				
3 RMSE	1.37836	1.80367	2.10263	
4 Theil's U	--	0.76419	0.65554	
5				
6 Diebold-Mariano Test				
7 DM	--	-2.24536	-2.57067	
8 P-value DM	--	0.03156	0.01485	
9 modified DM	--	-2.31340	-2.64857	
10 P-value modified DM	--	0.02707	0.01230	
11				
12 Chi^2 Independence				
13 Matching quota	0.66667	0.54545	0.21212	
14 Test statistic	3.47782	0.20263	11.38617	
15 P-value	0.06220	0.65261	0.00074	
16				
17 Test for Forecast Bias				
18 P-value a = 0	0.99388	0.07709	0.37020	
19 P-value b = 1	0.91121	0.06200	0.20444	
20 P-value joint	0.98810	0.14210	0.09640	
21				
22 Normal Distribution of Residuals				
23 Jarque-Bera	1.068896	0.031138	0.365587	
24 P-value	0.585993	0.984551	0.832940	
25				
26				
27				

## stage : additional features

- ❖ lag specification of  $\lambda$  is automatically chosen (,, , annual...)  
or can be imposed
- ❖ may also be used with equations containing quarterly regressors
- ❖ valuation of n-steps ahead forecasts
- ❖ test whether rolling optimization (for coefficients, variables and lags) improves forecasts
- ❖ many time series can be used as a benchmark (e.g. from external sources/models)
- ❖ forecasts of several equations can be computed and weighted (mean, median..)  
and then compared to a benchmark

## stage : **Automated forecasts**

- ❖ Automated forecasting tool for day-to-day use
- ❖ Exploit as much information as possible by considering all monthly regressors available

## stage : automated forecasts

- ❖ problem: monthly regressors are often only partially available within a given quarter
- dealing with staggered data: main-ridge equations to forecast missing data of monthly indicators
- ❖  $z_h$  denote auxiliary variables that won't be used in the main-ridge equation but are useful for forecasting the regressors  $x$
- ❖  $x_j$  are the variables to be forecasted:

$$A_j(L)x_{j,t} = \beta_{0,j} + \sum_{i \neq j} B_i(L)x_{i,t} + \sum_{h=1}^H C_h(L)z_{h,t} + \varepsilon_t \quad j = 1, 2, \dots, P$$

## tage : automated forecasts

- ❖ In order to find good auxiliary variables, tage . can be used with monthly dependent variables
- ❖ To find the optimal . ini-ridge equation, tage . can also be used

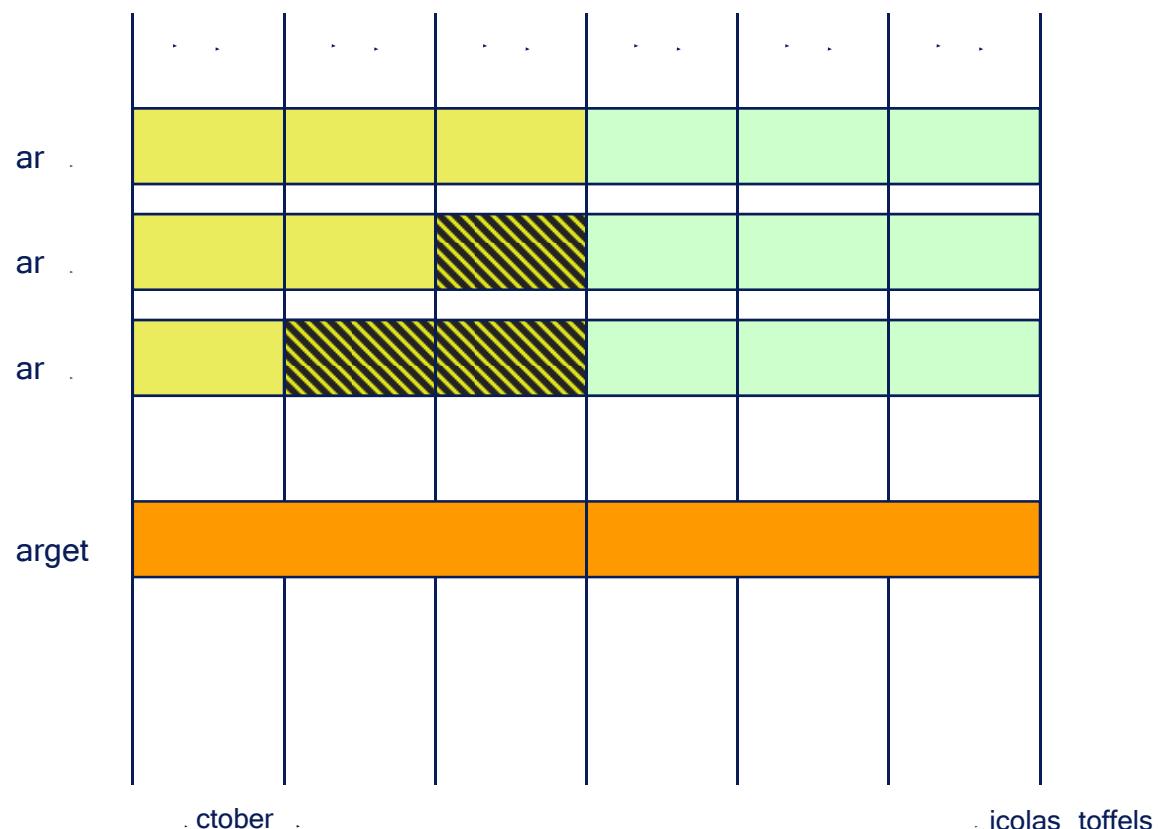
## stage : **automated forecasts**

- ❖ Once all exogenous variables have the same end date, a linear regression is estimated to compute a forecast up to the specified horizon
- ❖ Estimating then the best linear-ridge equation and computing a forecast
- ❖ Optionally: skipping the linear-ridge and linear forecasts and filling up the missing values with the mean of the previous month(s)



stage :

## Automated forecasts



- ini-ridge forecast (monthly)
- short-ridge forecast (monthly)
- main-ridge forecast (quarterly)

# Output: tage

Table: SUMMARY Workfile: OVERALL::...

	A	C	D	E	F	G	H
1	US GDP Growth Forecasts						
2							
3		2007Q3	2007Q4	2008Q1	2008Q2	Last Update	
4	@pca(gdp)	NA	NA	NA	NA		
5	Tracking_Mean	3.22	1.99	NA	NA	08/10/07 10:32	
6	Tracking_VAR	3.58	3.74	3.40	3.50	08/10/07 10:33	
7	Survey_Mean	2.46	2.75	2.54	2.92	08/10/07 10:32	
8	Survey_Median	2.70	2.92	2.68	2.91	08/10/07 10:32	
9	Harddata	2.58	3.21	3.04	3.10	08/10/07 10:33	
10	Top_1q	1.82	-0.77	NA	NA	08/10/07 10:33	
11	Leading_1q	2.29	2.72	1.99	2.88	08/10/07 10:34	
12	Top_2q	2.43	0.20	-0.37	NA	08/10/07 10:33	
13	Leading_2q	2.38	2.71	2.88	2.52	08/10/07 10:34	
17							
18							

## stage : pplication

- ❖ main-ridge:  
pca(gdp) c pca(gdp(-)) pca(pce) pca(ipman) pca(privconst)
- ❖ and construction data → main-ridge equations to forecast regressors
- ❖ auxiliary variables: retail sales, ours worked in construction
- ❖ number of tested main-ridge specifications: 1.
- ❖ \ to forecast monthly data up to q.
- ❖ computation time: . sec.

## stage : additional features

- ❖ forecasts with equations based on quarterly data
- ❖ forecasts where missing monthly data is completed with the mean of the previous month(s)
- ❖ **combination of forecasts:** can run a large set of forecasting equations and weight the results (mean, median...); useful assessment of the balance of risks

# Results

## Figure :

- ❖ Forecast accuracy significantly above benchmarks
- ❖ First month of data particularly important

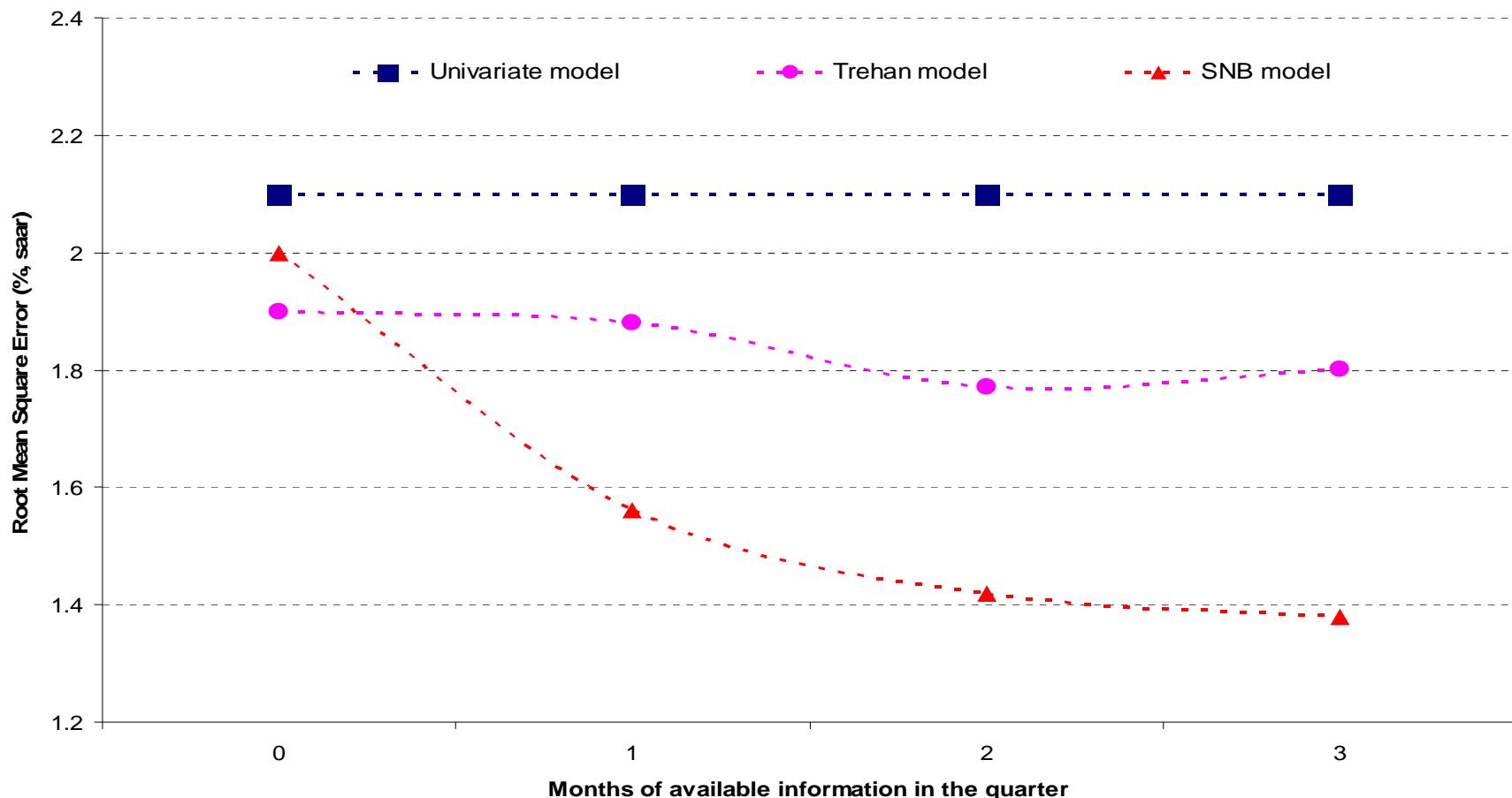
## Figure :

- ❖ fit-ratio above %; much higher than the univariate forecast
- ❖ fit-ratio *not* monotonously increasing with the information available



## Figure

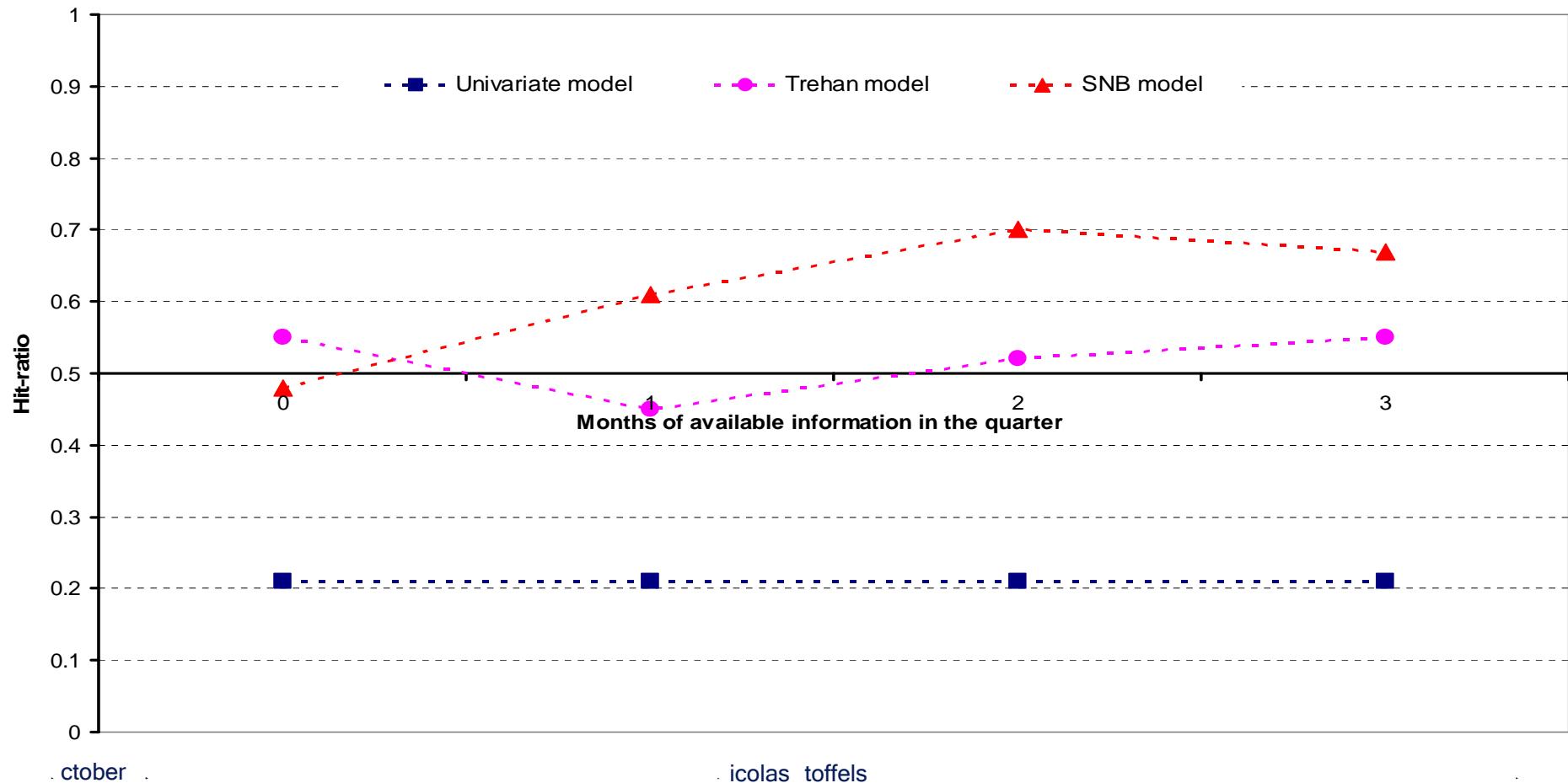
How does the model perform compared to benchmarks?  
(Sample: 1999q1-2007q2)





## Figure

Hit-ratio



Nicolas Toffels

## Results (contd)

Figure :

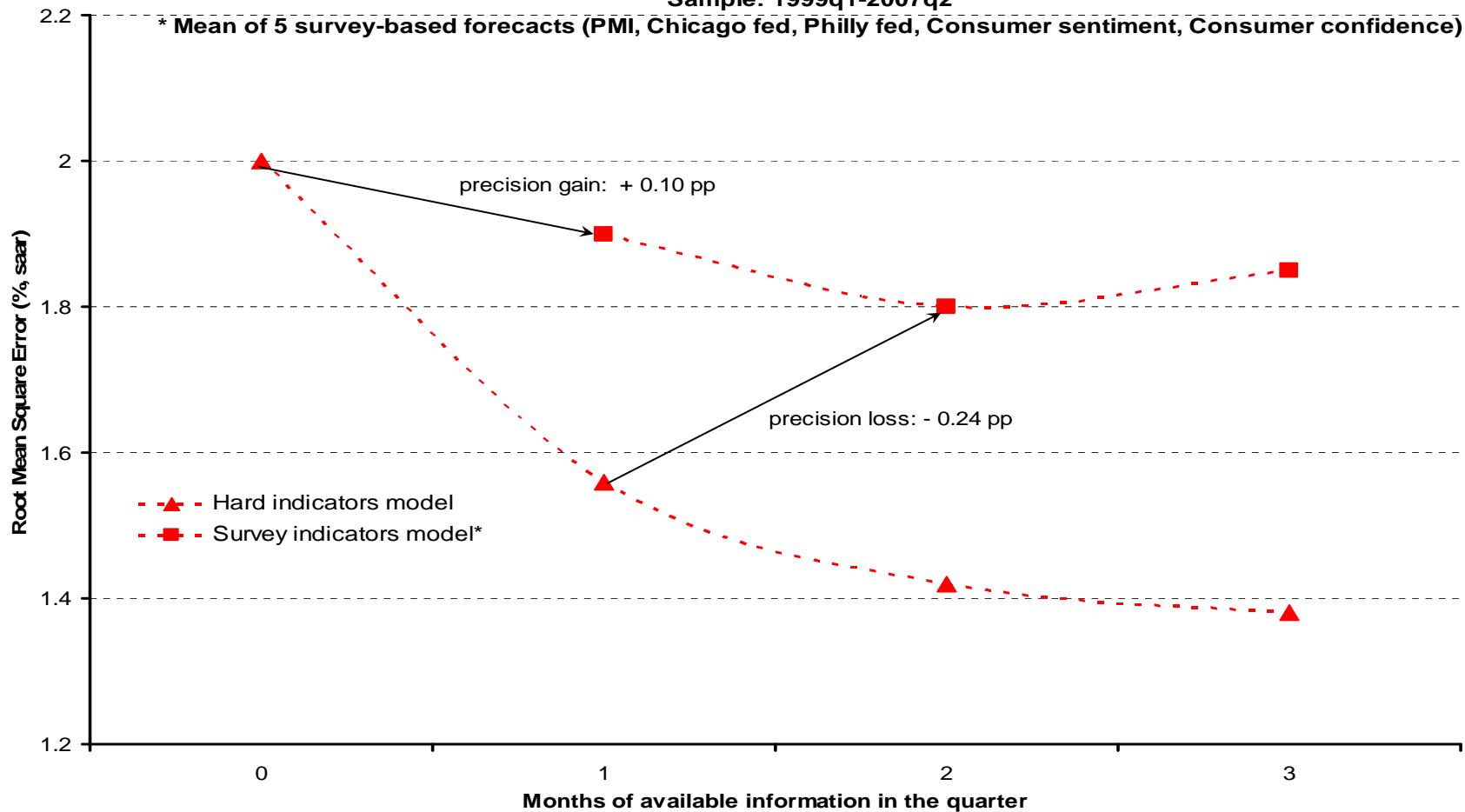
- ❖ Main point of using a survey-based model only until hard data arrive for the first month in the quarter



## Figure

## How much is it to gain from timely survey data ?

Sample: 1999q1-2007q2



## Results (contd)

### Figure :

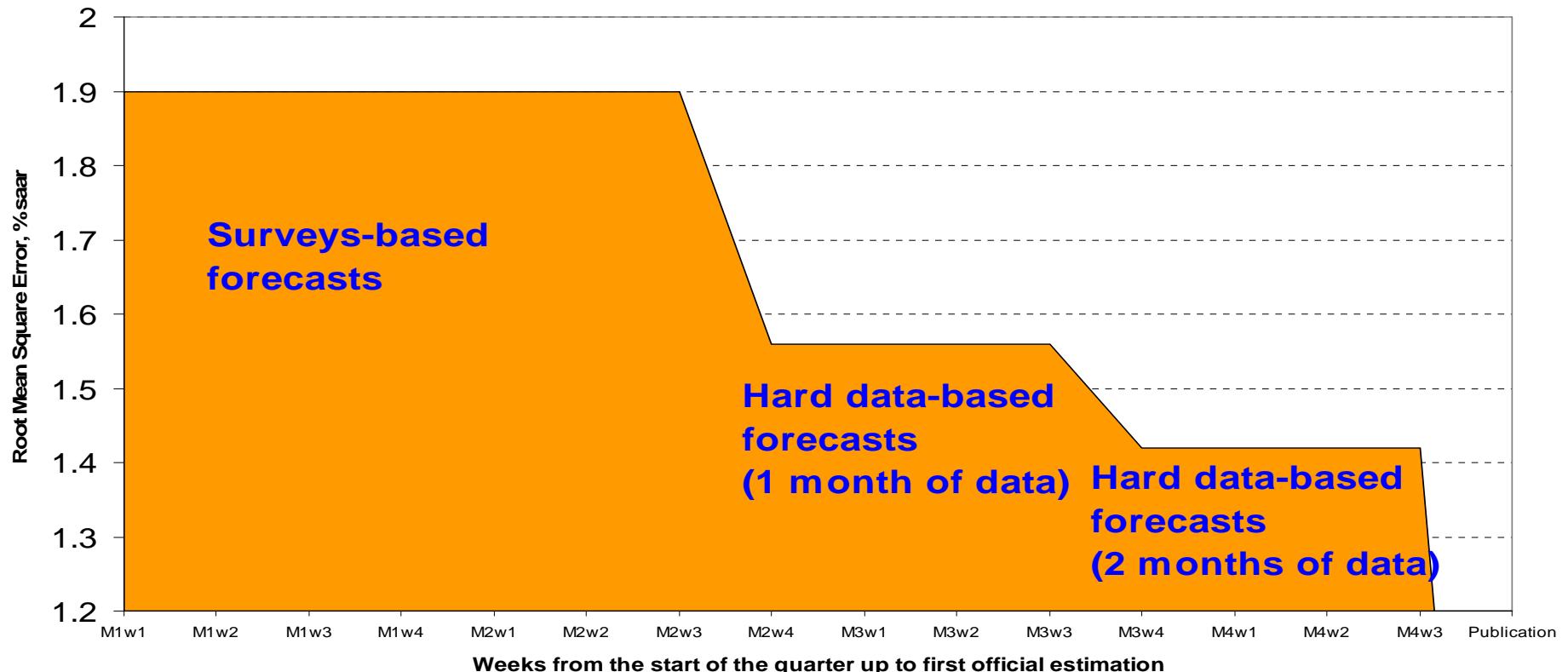
- ❖ Survey-based forecasts useful during the first half of current quarter
- ❖ Afterwards, better to incorporate information from the hard data
- ❖ Significant jump in accuracy when hard data become available
- ❖ Magnitude of errors very similar to the ones reported in recent interim forecasts document



# Figure 1

## Forecasting sequence

What type of model should be used throughout the quarter?



## summary

- ❖ potent tool to uncover variables with high informational content (tag 1 and 2)
- ❖ convenient way to evaluate out-of-sample forecasts based on various informational assumptions (tag 2)
- ❖ fast computing and summary of forecasts for daily use (tag 2)
- ❖ can compute and combine the results of a large set of forecasting equations