Data

Model

Quantification

Sensitivity Analysis

Do Financial Frictions Explain Chinese Firm Saving and Misallocation?

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Model

Motivation

- Literature emphasizes that financial frictions:
 - Generate high saving and outflow of capital
 - Song et al. (2011), Buera and Shin (2010), Mendoza et al.(2009)
 - Generate misallocation and low TFP
 - Hsieh and Klenow (2009), Midrigan and Xu (2014)
- We revisit the question: do financial frictions explain China's high saving and capital misallocation?
- Literature either uses aggregate data or ignores firms' financing patterns

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This Paper

- Use micro-level Chinese data to quantify financial frictions
- Study its implications on firms saving and capital misallocation
 - Focus on firm: firms saving account for 50 percent of total saving in China Firm Saving
- In terms of misallocation and TFP
 - Examine model generated MPK
 - Dispersion of MPK is not enough to measure misallocation
 - We argue that covariance between marginal product capital (MPK) and firm size matters for misallocation
 - Restuccia and Rogerson (2008): large TFP losses must be associated with positively correlated taxes and firm productivity

Empirical Findings

- Compared to SOE, POE
 - Have lower leverage
 - Pay higher interest rate
 - Grow faster
 - Have higher MPK
- Among POEs, relative to large firms, small firms
 - Have lower leverage
 - Pay higher interest rate
 - Grow faster
 - Have higher MPK

Note that these patterns are not easily reconcile with exogenous borrowing constraints, for example collateral constraints Motivation Data Model Quantification Sensitivity Analysis

Model with Endogenous Borrowing Constraints

- We develop a model with heterogenous firms and financial frictions including
 - Endogenous default risk
 - Fixed credit cost of borrowing
- Default risk generates endogenous borrowing constraints and differential interest rates across firms
- Higher credit cost leads to more correlated leverage and size

Quantify Financial Frictions in China

- We estimate the model with observed firm financing patterns and firm distribution
- Financial frictions can explain aggregate firm saving and co-movement between saving and investment across firms
- Financial frictions generate 60% of observed MPK dispersion, but an opposite MPK-size relationship
 - TFP loss depends on both dispersion and covariance
 - Intuitively, given the same MPK dispersion, whether subsidize small and tax large firms, or subsidize large and tax small, have different implications on TFP loss

	Litera	ature	

- Saving: Song et al. (2011), Buera and Shin (2010), Mendoza et al.(2009)
- Misallocation: Restuccia and Rogerson (2008), Restuccia and Rogerson (2013), Adamopoulos, Brandt, Leight, and Restuccia (2015), Hsieh and Klenow (2009), Midrigan and Xu (2014)
- Firm dynamics and financial frictions: Cooley and Quadrini (2001), Arellano, Bai, and Zhang (2010)

This paper: use micro level data and firm financing patterns to discipline financial frictions



- Balance sheet data 1998-2006
 - SOE: State Owned enterprises, including sole state funded, state joint ownership and state and collective joint ownership
 - POE: private enterprises, including sole private, private partnership, private limited liability and private shareholding corporations

Chinese Manufacturing Firms

- Key variables:
 - Leverage = $\frac{\text{liability}}{\text{asset}}$ Interest rate = $\frac{\text{interest payment}}{\text{liability}}$
 - Marginal product of capital

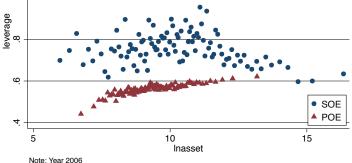
$$\log[MPK_{ij}] = \log(\alpha_j) + \log\left(\frac{Y_{ij}}{K_{ij}}\right)$$

 $\alpha_j:$ sector j average capital share or industry fixed effect

$$\log[MPK_{ij}] - \log[\overline{MPK_j}] = \log\left(\frac{Y_{ij}}{K_{ij}}\right) - \log\left(\frac{\overline{Y_j}}{K_j}\right)$$

 $\begin{array}{l} Y_{ij} : \mbox{ value added of firm } i \mbox{ at sector } j \\ K_{ij} : \mbox{ fixed asset of firm } i \mbox{ at sector } j \\ \hline \frac{Y_j}{K_j} : \mbox{ sector } j' \mbox{ sector } j' \mbox{ sector } j \mbox{ added-capital ratio } \end{array}$

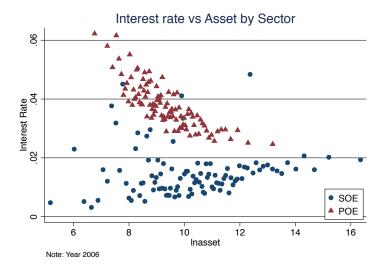




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Interest Rate and Size

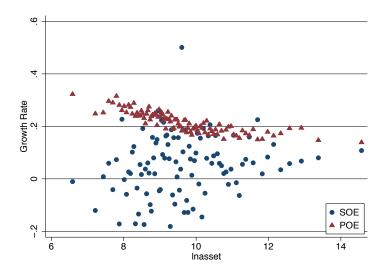


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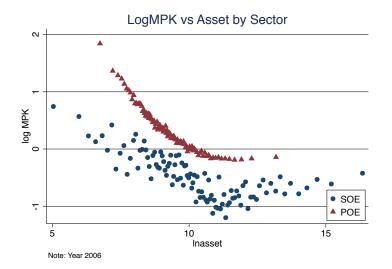
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Growth Rate and Size



MPK and Size



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Regression, Year 1999

	т	T + D +		1 MDV
	Leverage	Interest Rate	Growth Rate	$\log MPK$
lnasset	.036***	019***	029***	446***
	(6.65)	(-6.99)	(-3.87)	(-17.63)
SOE	.57***	215***	595***	-3.52***
	(9.38)	(-8.23)	(-7.63)	(-14.77)
SOE*lnasset	039***	.020***	.045***	0.261***
	(-7.35)	(7.36)	(5.4)	(9.94)
Observations	47,542	47,542	38,572	47,542
Industry FE	Yes	Yes	Yes	Yes
Robust t-statist	ice in parenth	eses *** p<0.01 '	** n<0.05 * n<0.1	

Robust t-statistics in parentheses. *** p<0.01, ** p<0.05, * p<0.1

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Regression, Year 2006

	Leverage	Interest Rate	Growth Rate	$\log MPK$
lnasset	.018***	006***	021***	341***
	(8.17)	(-3.68)	(-6.92)	(-26.59)
SOE	$.566^{***}$	089***	475***	-2.37***
	(11.58)	(-5.07)	(-7.13)	(-10.63)
SOE*lnasset	036***	.006***	$.033^{***}$	0.181***
	(-7.92)	(4.20)	(5.02)	(8.49)
Observations	142,009	142,009	112,368	142,009
Industry FE	Yes	Yes	Yes	Yes

Robust t-statistics in parentheses. *** p<0.01, ** p<0.05, * p<0.1

Sensitivity Analysis

Summary of Firm Level Data

- Compared to SOE, POE
 - Have lower leverage
 - Pay higher interest rate
 - Grow faster
 - Have higher MPK
- Among POEs, relative to large firms, small firms
 - Have lower leverage
 - Pay higher interest rate
 - Grow faster
 - Have higher MPK
- These patterns also hold for other years



- Note that these patterns are not easily reconcile with exogenous borrowing constraints
- Build a model with endogenous borrowing constraints
 - Discipline the model with firms financing patterns
- Examine firms saving, the MPK and misallocations under the model
 - The observed MPK could be affected by many other distortions

Data

A Simple Theory on Misallocation

- Heterogenous firms with $y_i = z_i^{1-\alpha} k_i^{\alpha}$
- From definition of MPK, $k_i = (\alpha)^{\frac{1}{1-\alpha}} z_i MPK_i^{\frac{1}{\alpha-1}}$
- TFP

$$TFP = \frac{Y}{K^{\alpha}} = \frac{\int_{i} z_{i} MPK_{i}^{\frac{\alpha}{\alpha-1}} d_{i}}{\left(\int_{i} z_{i} MPK_{i}^{\frac{1}{\alpha-1}} d_{i}\right)^{\alpha}}$$

• Efficient TFP: $MPK_i = MPK_j$

$$TFP^e = \left(\int_i z_i d_i\right)^{1-\alpha}$$

• TFP loss

TFP loss =
$$\log(TFP^e) - \log(TFP)$$

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Model

- Heterogenous firms in two sectors: SOE and POE
- Firms produce with DRS technology and finance investment and dividend payouts with internal funds and loans from banks
- Financial market is imperfect
 - Firms can only borrow state-uncontingent bond
 - SOEs are not allowed to default as long as they are able to repay their debts
 - POEs can default on their loans
 - Banks provide debt schedules taking into account default risks of firms and fixed cost of issuing loans



• Firms produce output using capital as input,

$$y = zk^{\alpha}$$

• z have a constant growth rate, a permanent component A_i , and an idiosyncratic component

$$z_{it} = (1+g)^t A_i \nu_{it}$$

• ν : following a Markov process given by $f(\nu'; \nu)$

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Model

POE Firms' Problem

- POEs can default over their loans b; after default
 - Still operate, but productivity reduced by γ fraction
 - Lose access to financial markets, λ prob. regain access
- Default decision

$$V(z,k,b) = \max_{d \in \{0,1\}} (1-d) V^{c}(z,k,b) + dV^{d}(z,k)$$

- d = 0 not default
- Defaulting value

$$V^{d}(z,k) = \max_{x,k'} x + \beta E \left[(1-\lambda) V^{d}(z',k') + \lambda V^{c}(z',k',0) \right]$$

st x = $(1-\gamma)zk^{\alpha} + (1-\delta)k - k' - \phi(k,k') \ge 0$



• Repaying value

$$V^{c}(z,k,b) = \max_{x,k',b'} \quad x + \beta EV(z',k',b')$$

st $x = zk^{\alpha} + (1-\delta)k - b + q(z,k',b')b' - k' - \phi(k,k') \ge 0$

• Debt price schedule q(z, k', b') reflects default risk



• SOE firms never default

$$W(z,k,b) = \max_{x,k',b'} x + \beta EW(z',k',b')$$

st $x = zk^{\alpha} + (1-\delta)k - b + q(z,k',b')b' - k' - \phi(k,k') \ge$
 $b' \le \bar{B}(z,k')$

• Nature borrow constraint guarantees the firms with the maximum borrowing limits are able to repay their debt



- Banks are competitive and risk neutral. Banks need to pay a fixed cost ξ for every loan they offer, which captures banks' overhead cost and the cost for obtaining information for each loan.
- For SOEs:

$$q(z, k', b') + \xi = \frac{1}{1+r}.$$

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- For POEs,
- When saving $b' \leq 0$ $q = \frac{1}{1+r}$
- When lending, have to pay a fixed cost ξ
- Prices reflect both default risk and fixed cost

$$q(z,k',b')b' + \xi = \frac{b'}{1+r} \left[1 - \int d(z',k',b') f(z';z) dz' \right].$$

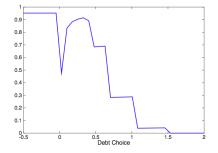


Definition: A recursive equilibrium consists of decision rules and value functions of firms, and bond price schedule q(z,k',b') such that

- 1. Given the bond price schedule, the decision rules and the value functions solve each firm's problem.
- 2. Given interest rate and the decision rules, the bond price schedule makes banks break even in expected value.

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- Small loans have high interest rate due to fixed cost
- Very large loans also have high interest rate due to default

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Shock structure

A firm's productivity

$$z_{it} = (1+g)^t A_i \nu_{it}$$

• Permanent A_i follows Pareto distribution

$$Pr(A_i \le x) = 1 - x^{-\mu}$$

• Idiosyncratic component ν_{it}

$$log(\nu_{it}) = \rho \log(\nu_{it-1}) + \sigma \varepsilon_{it}, \qquad \varepsilon_{it} \sim N(0, 1)$$

Model

Quantificatio

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Calibration

Calibrated Parameters	Value	Description
α	0.33	production function curvature
λ	0.1	reentry probability
δ	0.1	depreciation rate
r	0.05	riskfree rate
ho	0.85	persistence of productivity shock
		Gopinath et al (2015)
g	0.07	growth rate
Estimated Parameters		
β	0.94	discount factor
γ	0.3	output loss
ξ	0.012	fixed credit cost
ϕ	1.3	capital adjustment cost
σ	0.76	shock standard deviation
μ	1.30	shape parameter for permanent A
A_6	0.8	the second largest value of A
A_7	0.92	the largest value of A

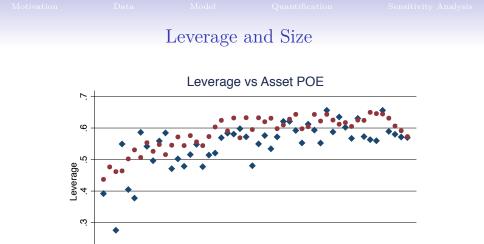
Model

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Model vs Data

		POE 1999	
Target Moments	Model	Data	
Leverage	0.56	0.58	
Leverage-Asset pct Slope	0.17	0.17	
Interest-Asset pct Slope	-0.12	-0.08	
Growth of value added			
Mean	0.14	0.13	
Var	0.40	0.40	
Distribution of value added			
TOP Percentiles	Fraction of value added		
5	0.34	0.34	
10	0.48	0.46	
20	0.66	0.62	



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model

Asset quantiles

.6

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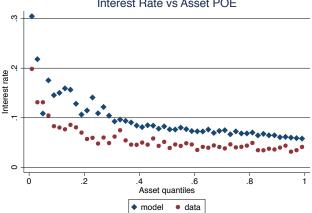
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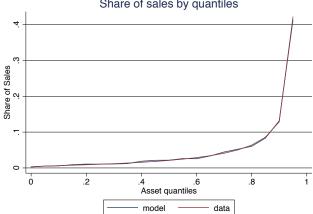
Interest Rate and Size



Interest Rate vs Asset POE

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Sales Distribution



Share of sales by quantiles

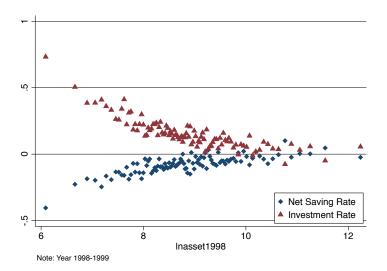
Model Implications on Saving

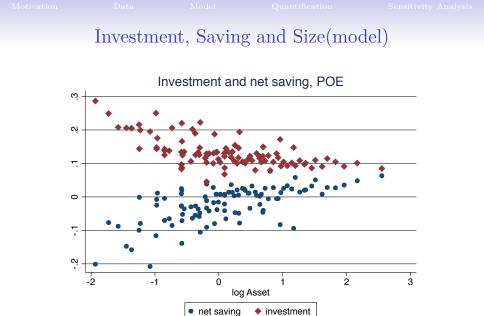
Non-Targeted Moments	Model	Data
Aggregate Statistics: Gross investment rate	0.15	0.18
Correlations		
Saving rate, Investment rate	0.28	0.58
Net saving rate, $\ln(asset)$	0.16	0.15

- Model generates co-movement of saving and investment
- Model matches well the co-movement of net saving and firms size

Motivation Data Model Quantification Sensitivity Analys

Investment, Saving and Size(Data)





Model Implications on MPK and Misallocation

Non-Targeted Moments	Model	Data
Aggregate Statistics:	0.67	1 10
Dispersion of MPK	0.67	1.12
Correlations		
MPK, asset	0.20	-0.36
MPK, leverage	0.36	0.01

- Model generates 60% of the observed MPK dispersion
- In the model, large firms have higher MPK. In the data, small firms have higher MPK due to other reasons

How MPK varies with size: rough intuition

$$E[MPK] = r + \delta + \underbrace{\phi f(K_{-1}, K)}_{\text{adjustment cost}} + \underbrace{\mu(A, K)}_{\text{financial frictions}}$$

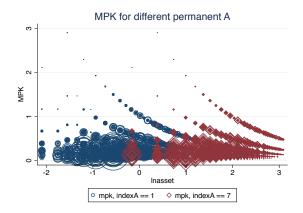
- Marginal adjustment cost $\phi f(K_{-1}, K)$ increases with K
- Financial friction $\mu(A, K)$ could
 - Increase with K: higher default incentive
 - Decrease with K: relax limited liability condition

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MPK across ν and A

- For each ν and A, MPK is downward sloping
- Within A, for different $\nu,$ MPK is upward sloping



Motivation

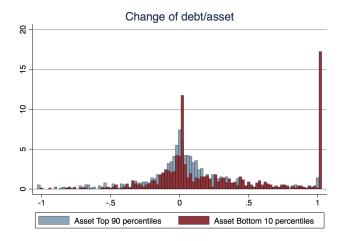
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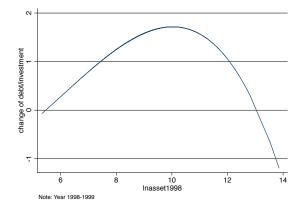
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Fixed Issuing Cost

In the data, small firms' change of debt are more lumpy







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In our model, financial friction generate 4.14% of TFP loss due to misallocation.

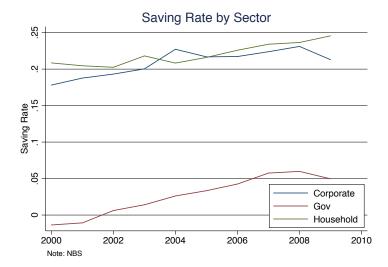
- Span of Control and Labor Market
 - In our benchmark $\alpha = 0.33$, freely adjusted labor
 - $\alpha = 0.85$ (larger loss)
- Capital adjustment cost
 - In our benchmark, convex adjustment cost (we leave firms investment rates for out of sample test) could generate too small variance of investment rate and too small TFP loss.
 - In the data, lumpy investment
- Misallocation between SOE and POE
- Large amount of entrants



- We document debt financing, interest spread, and growth of Chinese firms relate to firms size
- We use firm level data to quantify the effects of financial frictions on firm saving and misallocation
- We find that financial frictions
 - play important role in firms saving and investment decisions
 - generate capital misallocation (although not all the dispersion in the data)

Appendix

Saving Rates by Sectors





A Simple Theory on Misallocation

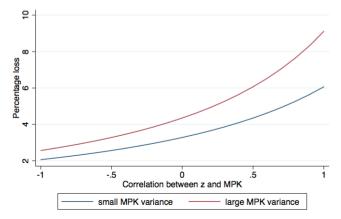
• Literature: z_i and MPK_i jointly log-normally distributed

TFP loss
$$= \frac{1}{2} \frac{\alpha}{1-\alpha} var(logMPK_i)$$

- TFP loss only depends on dispersion of MPK
- Generally covariance of z and MPK also matters Eg: Assume MPK is Pareto distributed with parameter γ , and $z = MPK^{\rho}$

TFP loss =
$$\frac{\gamma - \rho - \frac{\alpha}{\alpha - 1}}{(\gamma - \rho)^{1 - \alpha} \left(\gamma - \rho - \frac{1}{\alpha - 1}\right)^{\alpha}}$$

Example: TFP Loss Under Pareto Distribution



- Same dispersion of MPK, but TFP loss varies with size-MPK correlation
- High ρ leads to large TFP loss since high z accounts more for output